Junior Aviator Parents/Guardians,

The attached packet is for all 8th grade students that are in Mrs. Russo's Math classes. As you know, there has been a long-term substitute teaching these courses over the last two months. Until the school building reopens, the expectation is for your child to complete the attached packet. The reason for the hard-copy packet being sent home is because the long-term substitutes do not have a Google Classroom set up, as do the other classes. For these particular class periods, the students will NOT need to log in to a Google Classroom. However, they are still obligated to do so for their other courses.

All work must be shown for each section so that we could review and provide the necessary feedback where your child may have had difficulties. **Please note:** If you do not have the ability to print the attached Mathematics packet, your child may utilize notebook paper to do their work. This should be submitted upon our return to school. Please keep in mind that it is very important that all work is shown in order to receive full credit. If your child has any issues or problems with the packet, please encourage them to email me at mastropietroj@hhschools.org. I will be able to assist them. Also, I will also be emailing the students to check in on them while we are not in the building.

I want to thank you for your patience, collaboration, and support during this challenging time.

Respectfully,

Joseph Mastropietro

Joseph Mastropietro
Principal
Hasbrouck Heights Middle School

Rounding Decimals

Rounding Decimals

Round 8.135 to the nearest tenth.
$$8.1\underline{3}5 \rightarrow 8.1$$
less than 5

Round 32.56713 to the nearest hundredth.
$$32.56\underline{7}13 \rightarrow 32.57$$
greater than 5

Round to the nearest whole number.

1. 41.803 =

2. 119.63 =

3. 20.05 =

4. 3.45 =

5. 79.531 =

6. 8.437 =

7. 29.37 =

8. 109.96 =

Round to the nearest tenth.

9. 33.335 =

10. 1.861 =

11. 99.96 =

12. 103.103 =

13. 16.031 =

14. 281.05 =

15. 8.741 =

16. 27.773 =

Round to the nearest hundredth.

17. 69.713 =

18. 5.569 =

19. 609.906 =

20. 247.898 =

21. 5.535 =

22. 67.1951 =

23. 14.0305 =

24. 6.9372 =

Multiplying and Dividing by 10, 100, etc.

> When multiplying by a power of 10, move the decimal to the right:
> $34.61 \times 10 \rightarrow$ move 1 place $\rightarrow 346.1$
> $6.77 \times 100 \rightarrow$ move 2 places $\rightarrow 677$
>
> When dividing by a power of 10, move the decimal to the left:
> $7.39 \div 100 \rightarrow$ move 2 place $\rightarrow 0.0739$
> $105.61 \div 1000 \rightarrow$ move 3 places $\rightarrow 0.10561$

1. $4.81 \times 100 =$

2. $37.68 \div 10 =$

3. $0.46 \times 1,000 =$

4. $7.12 \div 10,000 =$

5. $5.4 \times 10 =$

6. $27,500 \div 1,000 =$

7. $4.395 \times 100,000 =$

8. $0.0075 \div 100 =$

9. $2.274 \times 10 =$

10. $90,000 \div 100 =$

11. $0.000618 \times 1,000 =$

12. $39.006 \div 1,000 =$

13. $16 \times 100 =$

14. $28.889 \div 10,000 =$

15. $36.89 \times 10,000 =$

16. $0.091 \div 100 =$

17. $0.0336 \times 100,000 =$

18. $1,672 \div 100,000 =$

0-7424-1787-5 Pre-Algebra
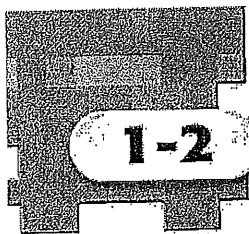
1-2 Study Guide and Intervention

Powers and Exponents

The **exponent** tells you how many times to use the **base** as a factor.

EXAMPLE 1 Write 6^3 as a product of the same factor.

The base is 6. The exponent 3 means that 6 is used as a factor 3 times.
$6^3 = 6 \cdot 6 \cdot 6$

EXAMPLE 2 Evaluate 5^4.

$5^4 = 5 \cdot 5 \cdot 5 \cdot 5$
$\quad = 625$

EXAMPLE 3 Write $4 \cdot 4 \cdot 4 \cdot 4 \cdot 4$ in exponential form.

The base is 4. It is used as a factor 5 times, so the exponent is 5.
$4 \cdot 4 \cdot 4 \cdot 4 \cdot 4 = 4^5$

EXERCISES

Write each power as a product of the same factor.

1. 7^3
2. 2^7
3. 9^2
4. 15^4

Evaluate each expression.

5. 3^5
6. 7^3
7. 8^4
8. 5^3

Write each product in exponential form.

9. $2 \cdot 2 \cdot 2 \cdot 2$

10. $7 \cdot 7 \cdot 7 \cdot 7 \cdot 7 \cdot 7$

11. $10 \cdot 10 \cdot 10$

12. $9 \cdot 9 \cdot 9 \cdot 9 \cdot 9$

13. $12 \cdot 12 \cdot 12$

14. $5 \cdot 5 \cdot 5 \cdot 5$

15. $6 \cdot 6 \cdot 6 \cdot 6 \cdot 6$

16. $1 \cdot 1 \cdot 1 \cdot 1 \cdot 1 \cdot 1 \cdot 1 \cdot 1$

1-3 Study Guide and Intervention

Order of Operations

Use the **order of operations** to evaluate numerical expressions.

1. Do all operations within grouping symbols first.
2. Evaluate all powers before other operations.
3. Multiply and divide in order from left to right.
4. Add and subtract in order from left to right.

EXAMPLE 1 Evaluate $(10 - 2) - 4 \cdot 2$.

$(10 - 2) - 4 \cdot 2 = 8 - 4 \cdot 2$ Subtract first since $10 - 2$ is in parentheses.
$\qquad\qquad\quad = 8 - 8$ Multiply 4 and 2.
$\qquad\qquad\quad = 0$ Subtract 8 from 8.

EXAMPLE 2 Evaluate $8 + (1 + 5)^2 \div 4$.

$8 + (1 + 5)^2 \div 4 = 8 + 6^2 \div 4$ First, add 1 and 5 inside the parentheses.
$\qquad\qquad\quad = 8 + 36 \div 4$ Find the value of 6^2.
$\qquad\qquad\quad = 8 + 9$ Divide 36 by 4.
$\qquad\qquad\quad = 17$ Add 8 and 9.

EXERCISES

Evaluate each expression.

1. $(1 + 7) \times 3$

2. $28 - 4 \cdot 7$

3. $5 + 4 \cdot 3$

4. $(40 \div 5) - 7 + 2$

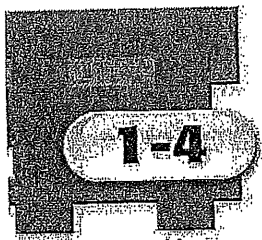5. $35 \div 7(2)$

6. 3×10^3

7. $45 \div 5 + 36 \div 4$

8. $42 \div 6 \times 2 - 9$

9. $2 \times 8 - 3^2 + 2$

10. $5 \times 2^2 + 32 \div 8$

11. $3 \times 6 - (9 - 8)^3$

12. 3.5×10^2

Lesson 1-3

1-4 Study Guide and Intervention

Adding Integers

To add integers with the same sign, add their absolute values. Give the result the same sign as the integers.

EXAMPLE 1 Find $-3 + (-4)$.

$-3 + (-4) = -7$ Add $|-3| + |-4|$. Both numbers are negative, so the sum is negative.

To add integers with different signs, subtract their absolute values. Give the result the same sign as the integer with the greater absolute value.

EXAMPLE 2 Find $-16 + 12$.

$-16 + 12 = -4$ Subtract $|12|$ from $|-16|$. The sum is negative because $|-16| > |12|$.

EXERCISES

Add.

1. $9 + 16$

2. $-10 + (-10)$

3. $18 + (-26)$

4. $-23 + (-15)$

5. $-45 + 35$

6. $39 + (-38)$

7. $-55 + 81$

8. $-61 + (-39)$

9. $-74 + 36$

10. $5 + (-4) + 8$

11. $-3 + 10 + (-6)$

12. $-13 + (-8) + (-12)$

13. $3 + (-10) + (-16) + 11$

14. $-17 + 31 + (-14) + 26$

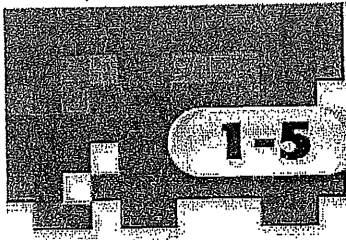**Evaluate each expression if $x = 4$ and $y = -3$.**

15. $11 + y$

16. $x + (-6)$

17. $y + 2$

18. $|x + y|$

19. $|x| + y$

20. $x + |y|$

1-5 Study Guide and Intervention

Subtracting Integers

To subtract an integer, add its opposite or additive inverse.

EXAMPLE 1 Find $8 - 15$.

$$8 - 15 = 8 + (-15) \quad \text{To subtract 15, add } -15.$$
$$= -7 \quad \text{Add.}$$

EXAMPLE 2 Find $13 - (-22)$.

$$13 - (-22) = 13 + 22 \quad \text{To subtract } -22, \text{ add 22.}$$
$$= 35 \quad \text{Add.}$$

EXERCISES

Subtract.

1. $-3 - 4$

2. $5 - (-2)$

3. $-10 - 8$

4. $-15 - (-12)$

5. $-23 - (-28)$

6. $16 - 9$

7. $9 - 16$

8. $-21 - 16$

9. $28 - 37$

10. $-34 - (-46)$

11. $65 - (-6)$

12. $19 - |29|$

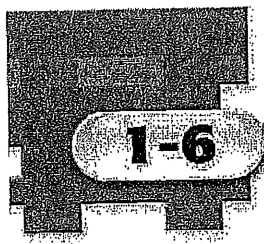Evaluate each expression if $a = -7$, $b = -3$, and $c = 5$.

13. $a - 8$

14. $20 - b$

15. $a - c$

16. $c - b$

17. $b - a - c$

18. $c - b - a$

1-6 Study Guide and Intervention

Multiplying and Dividing Integers

Use the following rules to determine whether the product or quotient of two integers is positive or negative.
- The product of two integers with different signs is negative.
- The product of two integers with the same sign is positive.
- The quotient of two integers with different signs is negative.
- The quotient of two integers with the same sign is positive.

EXAMPLE 1 Find $7(-4)$.

$7(-4) = -28$ The factors have different signs. The product is negative.

EXAMPLE 2 Find $-5(-6)$.

$-5(-6) = 30$ The factors have the same sign. The product is positive.

EXAMPLE 3 Find $15 \div (-3)$.

$15 \div (-3) = -5$ The dividend and divisor have different signs. The quotient is negative.

EXAMPLE 4 Find $-54 \div (-6)$.

$-54 \div (-6) = 9$ The dividend and divisor have the same sign. The quotient is positive.

EXERCISES

Multiply or divide.

1. $8(-8)$

2. $-3(-7)$

3. $-9(4)$

4. $12(8)$

5. $33 \div (-3)$

6. $-25 \div 5$

7. $48 \div 4$

8. $-63 \div (-7)$

9. $(-4)^2$

10. $\dfrac{-75}{15}$

11. $-6(3)(-5)$

12. $\dfrac{-143}{-13}$

Evaluate each expression if $a = -1$, $b = 4$, and $c = -7$.

13. $3c + b$

14. $a(b + c)$

15. $c^2 - 5b$

16. $\dfrac{a - 6}{c}$

7

2-3 Study Guide and Intervention

Multiplying Rational Numbers

To multiply fractions, multiply the numerators and multiply the denominators.

EXAMPLE 1 Find $\frac{3}{8} \cdot \frac{4}{11}$. Write in simplest form.

$$\frac{3}{8} \cdot \frac{4}{11} = \frac{3}{\overset{}{\underset{2}{8}}} \cdot \frac{\overset{1}{4}}{11} \qquad \text{Divide 8 and 4 by their GCF, 4.}$$

$$= \frac{3 \cdot 1}{2 \cdot 11} \qquad \text{Multiply the numerators and denominators.}$$

$$= \frac{3}{22} \qquad \text{Simplify.}$$

To multiply mixed numbers, first rewrite them as improper fractions.

EXAMPLE 2 Find $-2\frac{1}{3} \cdot 3\frac{3}{5}$. Write in simplest form.

$$-2\frac{1}{3} \cdot 3\frac{3}{5} = -\frac{7}{3} \cdot \frac{18}{5} \qquad -2\frac{1}{3} = -\frac{7}{3}, \ 3\frac{3}{5} = \frac{18}{5}$$

$$= -\frac{7}{\underset{1}{3}} \cdot \frac{\overset{6}{18}}{5} \qquad \text{Divide 18 and 3 by their GCF, 3.}$$

$$= -\frac{7 \cdot 6}{1 \cdot 5} \qquad \text{Multiply the numerators and denominators.}$$

$$= -\frac{42}{5} \qquad \text{Simplify.}$$

$$= -8\frac{2}{5} \qquad \text{Write the result as a mixed number.}$$

EXERCISES

Multiply. Write in simplest form.

1. $\frac{2}{3} \cdot \frac{3}{5}$ 　　　　　　2. $\frac{4}{7} \cdot \frac{3}{4}$ 　　　　　　3. $-\frac{1}{2} \cdot \frac{7}{9}$

4. $\frac{9}{10} \cdot \frac{2}{3}$ 　　　　　　5. $\frac{5}{8} \cdot \left(-\frac{4}{9}\right)$ 　　　　　　6. $-\frac{4}{7} \cdot \left(-\frac{2}{3}\right)$

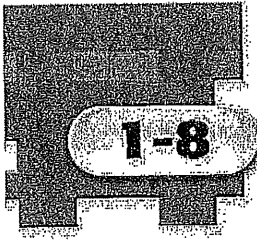7. $2\frac{2}{5} \cdot \frac{1}{6}$ 　　　　　　8. $-3\frac{1}{3} \cdot 1\frac{1}{2}$ 　　　　　　9. $3\frac{3}{7} \cdot 2\frac{5}{8}$

10. $-1\frac{7}{8} \cdot \left(-2\frac{2}{5}\right)$ 　　　　11. $-1\frac{3}{4} \cdot 2\frac{1}{5}$ 　　　　12. $2\frac{2}{3} \cdot 2\frac{3}{7}$

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Lesson 2-3

1-8 Study Guide and Intervention

Solving Addition and Subtraction Equations

You can use the following properties to solve addition and subtraction equations.
- *Addition Property of Equality* - If you add the same number to each side of an equation, the two sides remain equal.
- *Subtraction Property of Equality* - If you subtract the same number from each side of an equation, the two sides remain equal.

EXAMPLE 1 Solve $w + 19 = 45$. Check your solution.

$$w + 19 = 45 \qquad \text{Write the equation.}$$
$$w + 19 - 19 = 45 - 19 \qquad \text{Subtract 19 from each side.}$$
$$w = 26 \qquad 19 - 19 = 0 \text{ and } 45 - 19 = 26.\ w \text{ is by itself.}$$

Check
$$w + 19 = 45 \qquad \text{Write the original equation.}$$
$$26 + 19 \overset{?}{=} 45 \qquad \text{Replace } w \text{ with 26. Is this sentence true?}$$
$$45 = 45 \checkmark \qquad 26 + 19 = 45$$

EXAMPLE 2 Solve $h - 25 = -76$. Check your solution.

$$h - 25 = -76 \qquad \text{Write the equation.}$$
$$h - 25 + 25 = -76 + 25 \qquad \text{Add 25 to each side.}$$
$$h = -51 \qquad -25 + 25 = 0 \text{ and } -76 + 25 = -51.\ h \text{ is by itself.}$$

Check
$$h - 25 = -76 \qquad \text{Write the original equation.}$$
$$-51 - 25 \overset{?}{=} -76 \qquad \text{Replace } h \text{ with } -51. \text{ Is this sentence true?}$$
$$-76 = -76 \checkmark \qquad -51 - 25 = -51 + (-25) \text{ or } -76$$

EXERCISES

Solve each equation. Check your solution.

1. $s - 4 = 12$

2. $d + 2 = 21$

3. $h + 6 = 15$

4. $x + 5 = -8$

5. $b - 10 = -34$

6. $f - 22 = -6$

7. $17 + c = 41$

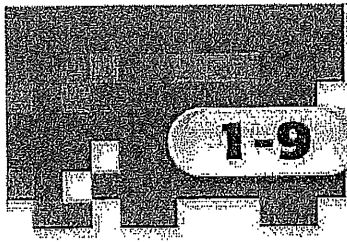8. $v - 36 = 25$

9. $y - 29 = -51$

10. $19 = z - 32$

11. $13 + t = -29$

12. $55 = 39 + k$

13. $62 + b = 45$

14. $x - 39 = -65$

15. $-56 = -47 + n$

1-9 Study Guide and Intervention

Solving Multiplication and Division Equations

You can use the following properties to solve multiplication and division equations.

- *Multiplication Property of Equality* - If you multiply each side of an equation by the same number, the two sides remain equal.
- *Division Property of Equality* - If you divide each side of an equation by the same nonzero number, the two sides remain equal.

EXAMPLE 1 Solve $19w = 104$. Check your solution.

$$19w = 114 \qquad \text{Write the equation.}$$

$$\frac{19w}{19} = \frac{114}{19} \qquad \text{Divide each side of the equation by 19.}$$

$$1w = 6 \qquad 19 \div 19 = 1 \text{ and } 114 \div 19 = 6.$$

$$w = 6 \qquad \text{Identity Property; } 1w = w$$

Check $\quad 19w = 114 \qquad$ Write the original equation.

$\qquad 19(6) \stackrel{?}{=} 114 \qquad$ Replace w with 6.

$\qquad 114 = 114 \checkmark \qquad$ This sentence is true.

EXAMPLE 2 Solve $\frac{d}{15} = -9$. Check your solution.

$$\frac{d}{15} = -9$$

$$\frac{d}{15}(15) = -9(15) \qquad \text{Multiply each side of the equation by 15.}$$

$$d = -135$$

Check $\quad \frac{d}{15} = -9 \qquad$ Write the original equation.

$\qquad \frac{-135}{15} \stackrel{?}{=} -9 \qquad$ Replace d with -135.

$\qquad -9 = -9 \checkmark \qquad -135 \div 15 = -9$

EXERCISES

Solve each equation. Check your solution.

1. $\frac{r}{5} = 6$

2. $2d = 12$

3. $7h = -21$

4. $-8x = 40$

5. $\frac{f}{8} = -6$

6. $\frac{x}{-10} = -7$

7. $17c = -68$

8. $\frac{h}{-11} = 12$

9. $29t = -145$

10. $125 = 5z$

11. $13t = -182$

12. $117 = -39k$

Lesson 1-9
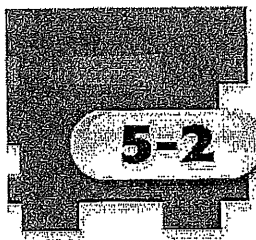
5-2 Study Guide and Intervention

Fractions, Decimals, and Percents

- To write a percent as a decimal, divide by 100 and remove the percent symbol.
- To write a decimal as a percent, multiply by 100 and add the percent symbol.
- To express a fraction as a percent, you can use a proportion. Alternatively, you can write the fraction as a decimal, and then express the decimal as a percent.

EXAMPLE 1 Write 56% as a decimal.

$56\% = 56\%$ Divide by 100 and remove the percent symbol.

$= 0.56$

EXAMPLE 2 Write 0.17 as a percent.

$0.17 = 0.17$ Multiply by 100 and add the percent symbol.

$= 17\%$

EXAMPLE 3 Write $\frac{7}{20}$ as a percent.

Method 1 Use a proportion.

$$\frac{7}{20} = \frac{x}{100}$$ Write the proportion.

$7 \cdot 100 = 20 \cdot x$ Find cross products.

$700 = 20x$ Multiply.

$$\frac{700}{20} = \frac{20x}{20}$$ Divide each side by 20.

$35 = x$ Simplify.

Method 2 Write as a decimal.

$\frac{7}{20} = 0.35$ Convert to a decimal by dividing.

$= 35\%$ Multiply by 100 and add the percent symbol.

So, $\frac{7}{20}$ can be written as 35%.

EXERCISES

Write each percent as a decimal.

1. 10%

2. 36%

3. 82%

4. 49.1%

Write each decimal as a percent.
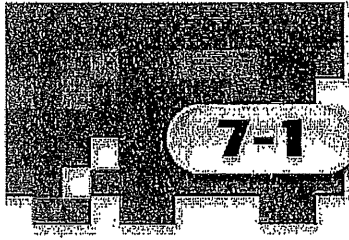
5. 0.14

6. 0.59

7. 0.932

8. 1.07

Write each fraction as a percent.

9. $\frac{3}{4}$

10. $\frac{7}{10}$

11. $\frac{9}{16}$

12. $\frac{1}{40}$

7-1 Study Guide and Intervention

Area of Parallelograms, Triangles, and Trapezoids

The area A of a parallelogram is the product of any base b and its height h, or $A = bh$.

The area A of a triangle is half the product of any base b and its height h, or $A = \frac{1}{2}bh$.

The area A of a trapezoid is half the product of the height h and the sum of the bases, b_1 and b_2, or $A = \frac{1}{2}h(b_1 + b_2)$.

EXAMPLES Find the area of each figure.

1 The base is 8 yards. The height is 6 yards.

$A = bh$ Area of a parallelogram

$A = 8 \cdot 6$ or 48   Replace b with 8 and h with 6. Multiply.

The area is 48 square yards.

6 yd
8 yd
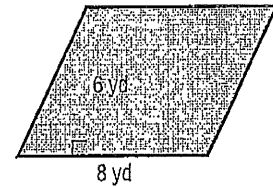
2 The base is 10 feet. The height is 4 feet.

$A = \frac{1}{2}bh$ Area of a triangle

$A = \frac{1}{2} \cdot 10 \cdot 4$ or 20   Replace b with 10 and h with 4. Multiply.

The area is 20 square feet.

10 ft
4 ft
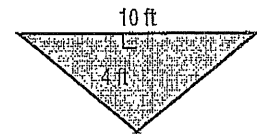
3 The height is 5 inches. The lengths of the bases are 9 inches and 7 inches.

$A = \frac{1}{2}h(b_1 + b_2)$ Area of a trapezoid

$A = \frac{1}{2} \cdot 5 \cdot (9 + 7)$ or 40   Replace h with 5, b_1 with 9, and b_2 with 7. Simplify.

The area is 40 square inches.

9 in.
5 in.
7 in.
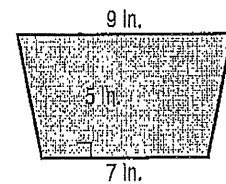
EXERCISES

Find the area of each figure.
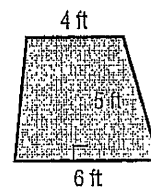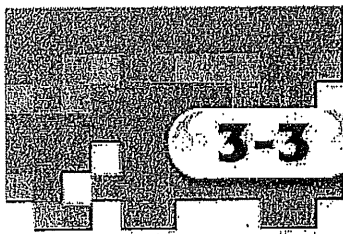
1.
9 m
8 m

2.
4 yd
6 yd

3.
4 ft
5 ft
6 ft
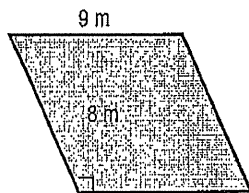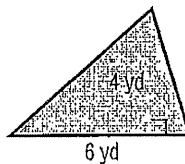
4. parallelogram: base, 11 cm; height, 12 cm

5. triangle: base, 8 mi; height, 13 mi

6. trapezoid: height, 7 km; bases, 8 km and 12 km

Mathematics: Applications and Concepts, Course 3

Lesson 7-1

## 3-3 Study Guide and Intervention

The Coordinate Plane

The **coordinate plane** is used to locate points. The horizontal number line is the **x-axis**. The vertical number line is the **y-axis**. Their intersection is the **origin**.

Points are located using **ordered pairs**. The first number in an ordered pair is the **x-coordinate**; the second number is the **y-coordinate**.

The coordinate plane is separated into four sections called **quadrants**.

EXAMPLE 1 Name the ordered pair for point P. Then identify the quadrant in which P lies.

- Start at the origin.
- Move 4 units left along the x-axis.
- Move 3 units up on the y-axis.
  The ordered pair for point P is (−4, 3).
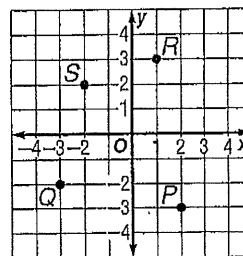 P is in the upper left quadrant or quadrant II.
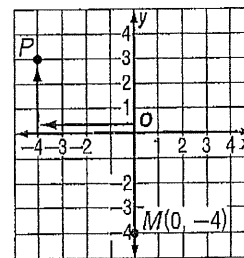
EXAMPLE 2 Graph and label the point M(0, −4).

- Start at the origin.
- Move 0 units along the x-axis.
- Move 4 units down on the y-axis.
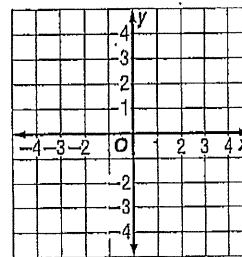- Draw a dot and label it M(0, −4).

EXERCISES

Name the ordered pair for each point graphed at the right. Then identify the quadrant in which each point lies.

1. P

2. Q

3. R

4. S

Graph and label each point on the coordinate plane.

5. A(−1, 1)

6. B(0, −3)

7. C(3, 2)

8. D(−3, −1)

9. E(1, −2)

10. F(1, 3)

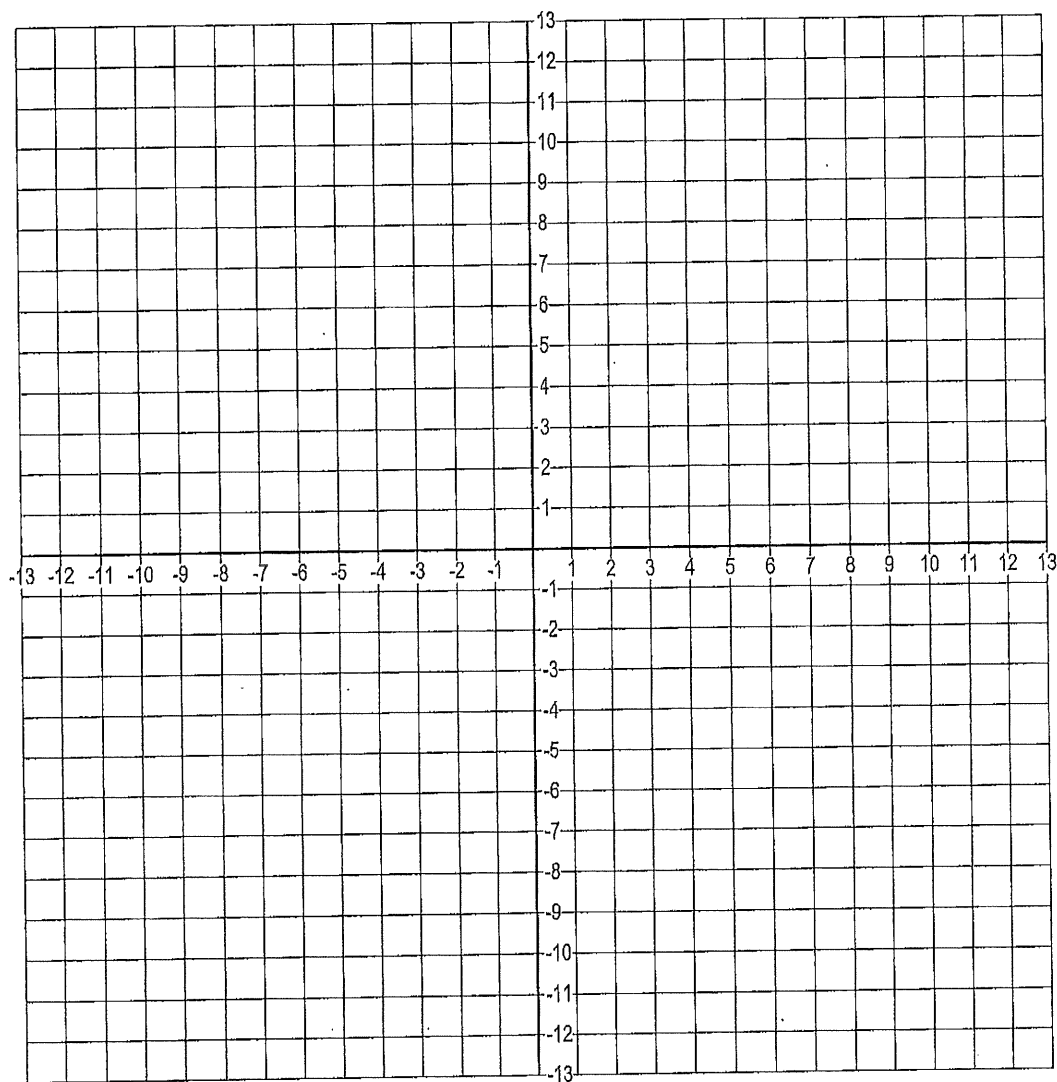Lesson 3-3

Plotting a Hidden Message

Name: _____ **Date:** _____

☞ Connect each series of points to reveal a hidden message.

(−12,4)(−12,0) (6,−5)(4,−5)(4,−1)(6,−1) (−3,0)(−5,0)(−5,4)(−3,4) (−6,5)(−8,5)(−8,9)(−6,9)
(10,2)(12,2) (3,−8)(5,−8) (4,−3)(5,−3) (0,−6)(2,−6) (−2,4)(0,4) (4,0)(4,4) (−2,0)(0,0)
(−6,−10)(−6,−6)(−5,−9)(−4,−6)(−4,−10) (−6,−1)(−8,−2)(−8,−4)(−6,−5)(−6,−3)(−7,−3) (7,7)(8,7)
(−5,−5)(−5,−1)(−3,−1)(−3,−3)(−5,−3) (−11,9)(−11,5)(−10,7)(−9,5)(−9,9) (9,5)(7,5)(7,9)(9,9)
    (1,5)(1,9)(3,9)(3,5)(1,5) (3,4)(1,3)(1,1)(3,0)(3,2)(2,2) (4,5)(4,9)(5,6)(6,9)(6,5)
(−8,7)(−7,7) (−5,9)(−5,5)(−3,5) (1,−6)(1,−10) (−3,−8)(−1,−8) (−4,−3)(−3,−5) (−2,−3)(0,−3)
(−13,4)(−11,4) (1,−5)(1,−1)(2,−1)(3,−3)(2,−5)(1,−5) (−3,−10)(−3,−8)(−2,−6)(−1,−8)(−1,−10)
    (5,−10)(5,−6) (12,0)(12,4) (10,0)(10,4) (−1,0)(−1,4) (3,−10)(3,−6) (−5,2)(−4,2)
(−2,−5)(−2,−3)(−1,−1)(0,−3)(0,−5) (0,5)(−2,5)(−2,9)(0,9) (−10,0)(−10,4)(−8,4)(−8,0)(−10,0)
            (8,4)(8,0) (4,2)(6,2) (7,4)(9,4) (6,0)(6,4)